ECO6143 Natural-Resource Economics Mid-term exam October 12 2007 Professor: Louis Hotte Time allowed: 2 hours

## 1. Review question (50 points)

In the case of a fishery, show how it is possible to have a higher steady-state output with open-access than exclusive ownership, even though the latter is more efficient than the former. Explain. (NB Analyze this in the context of a simple steady-state framework, i.e. as when the discount *rate* is equal to zero.)

## 2. (50 points) A dynamic, discrete-time analysis of a fishery with ecological stock value

The natural growth of a fish stock during any year t is given by a logistic function denoted  $F(S_t)$ , where  $S_t$  is the fish stock size in tons at the beginning of year t. With a year t harvested quantity of  $H_t$  tons, the change in stock size between two years is

(1) 
$$S_{t+1} - S_t = F(S_t) - H_t.$$

The cost of harvest is expressed as  $C(H_t, S_t)$ , with  $C_H(H_t, S_t) > 0$  and  $C_S(H_t, S_t) < 0$ . The unit selling price of a ton of fish is constant over time and equal to p; this represents its *direct* commercial value.

The fish stock size also contributes to the marine ecological equilibrium. This has repercussions over the commercial value of other species, bio-diversity, amenity values for divers, etc. To make things simple, let us say that the lower our fish stock  $S_t$ , the more adversely affected is the ecological equilibrium and thus the *indirect* social value of the fish stock. Formally, we represent this indirect social value by  $U(S_t)$ , with  $U'(S_t) > 0$ ,  $U''(S_t) < 0$ .

During any period t, the net flow of social benefits generated by the fish stock is thus given by  $b_t = U(S_t) + pH_t - C(H_t, S_t)$ .

- a) For an infinite number of future periods, solve for the present value maximization of the sum of social benefits that would be chosen by a benevolent social planner. Assume a yearly social discount *factor* equal to  $\beta = 1/(1 + r)$ . Interpret fully the optimality condition.
- b) Characterize the steady-state stock of the resource which corresponds to present value maximization in a.
- c) Analyze and discuss the effect of a technological improvements in harvesting technology by assuming that harvesting costs become negligible, i.e.  $C(H_t, S_t) = 0$ , and comparing with the previous solution.
- d) Discuss how the introduction of an indirect stock social value is likely to affect the steadystate exploitation of the fishery when one compares the problem of a profit-maximizing firm with that of a social planner. (Assume that both use the same discount factor.)
- e) How does the steady-state stock level found in b compare with the MSY stock level? Discuss.